

IV B.Tech II Semester Regular Examinations, Apr/May 2006

**FINITE ELEMENT METHODS**

( Common to Mechanical Engineering and Production Engineering)

Time: 3 hours

Max Marks: 80

Answer any FIVE Questions  
All Questions carry equal marks

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1. Write notes on the following:
  - (a) Weighted Residual method.
  - (b) Initial and Boundary value problems. [8+8]
2. With a suitable example explain the formulation of finite element equations by direct approach. Assume suitable data for the example. Use I-D analysis. [16]
3. Define and derive the Hermite shape functions for a two noded beam element? [16]
4. (a) Show that the value of the shape function  $N_1$  of node i and node k of a simplex triangular element is zero and at node I is one.  
(b) The (x, y) coordinates of the nodes i, j and k of a triangular element are (1, 1), (4, 2) and (3, 5) respectively. The shape functions of a point P located inside the element are given by  $N_1 = 0.15$  and  $N_2 = 0.25$ . Determine the x and y coordinates of the point P. [6+10]
5. Derive the conductivity matrix and vector for the 2-D element when one of the faces is exposed to a heat transfer coefficient of h at  $T_\infty$  and with internal heat generation of q W/m<sup>3</sup>. [16]
6. Explain the following with examples.
  - (a) Lumped parameter model.
  - (b) Continuous system model. [8+8]
7. Write a procedure for model creation and mesh generation for aerofoil shape turbine blades. [16]
8. Give the necessity of rotating and offsetting the work plane in ANSYS environment. What are the useful features of CAEFEM package in analysis? [16]

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- Explain the following with neat sketches.
  - Mathematical Finite Element method.
  - Physical Finite Element Method. [8+8]
- Explain the mathematical interpretation of finite element method for one dimensional field problems. [16]
- For the pin jointed truss shown in figure1. If  $E = 200 \text{ Gpa}$ , determine
  - Element stiffness matrices .
  - Global stiffness matrix .
  - Stress in the element 1.
  - Strain in the element 2. [6+4+3+3]

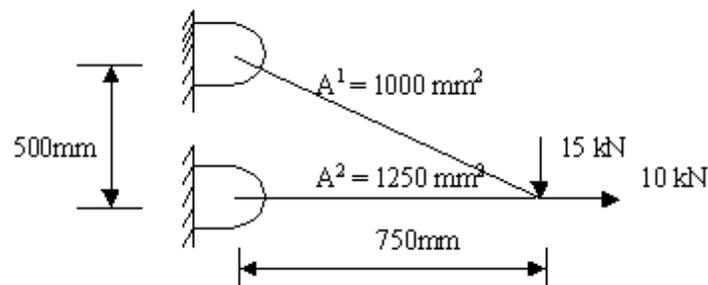


Figure 1:

- Show that the value of the shape function  $N_1$  of node i and node k of a simplex triangular element is zero and at node I is one.
  - The  $(x, y)$  coordinates of the nodes i, j and k of a triangular element are  $(1, 1)$ ,  $(4, 2)$  and  $(3, 5)$  respectively. The shape functions of a point P located inside the element are given by  $N_1 = 0.15$  and  $N_2 = 0.25$ . Determine the x and y coordinates of the point P. [6+10]
- Explain the methodology for the treatment of all three boundary conditions in a 1-D heat transfer element? [16]

6. Find the natural frequencies and the corresponding mode shapes for the longitudinal vibrations for the stepped bar. Assume  $A_1 = 2A$  and  $A_2 = A$  ;  $I_1 = I_2 = I$  ;  $E_1 = E_2 = E$ . [16]
7. When will a finite element is called an element from the Lagrange family? Establish shape functions and write Jacobian matrix for any two, three dimensional elements of Lagrange family. [6+5+5]
8. (a) Describe  $C^0$  , $C^1$  , $C^2$  classes.  
(b) Write features of the ANSYS, NISA, NASTRAN. [8+8]

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1. Derive the various equations for static equilibrium of an elastic body. [16]
2. With a suitable example explain the formulation of finite element equations by direct approach. Assume suitable data for the example. Use I-D analysis. [16]
3. Derive the methodology to develop a stiffness matrix and load vector for a 2-noded beam element with 2 degree of freedom? [16]
4. (a) Derive strain displacement [B] matrix for a 3 noded Triangular element?  
(b) The nodal coordinates and the nodal displacements of a triangular element, under a specific load condition are given below:  
 $X_i = 0, Y_i = 0, X_j = 1 \text{ mm}, Y_j = 3 \text{ mm}, X_k = 4 \text{ mm}, Y_k = 1, u_1 = 1 \text{ mm},$   
 $u_2 = -0.05 \text{ mm}, u_3 = 2 \text{ mm}, V_1 = 0.5 \text{ mm}, V_2 = 1.5 \text{ mm}$  and  $V_3 = -1 \text{ mm}$ . If  $E = 2 \times 10^5 \text{ N/mm}^2$  and  $\mu = 0.3$ . find the stresses in the element. [8+8]
5. Discuss the finite element methodology to solve the torsion problems from the first principles? [16]
6. Explain the following with examples.
  - (a) Lumped parameter model.
  - (b) Continuous system model. [8+8]
7. (a) Derive the shape functions for a Hexahedral element.  
(b) Explain the various convergence requirements. [8+8]
8. What are the advantages and limitations of NISA Package over ANSYS, CAEFEM and NASTRAN? [16]

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1. With the help of a neat diagram, describe the various components of stress and strains. [4+6+6]
2. With a suitable example, explain the physical interpretation of finite element method for one dimensional analysis. [16]
3. Find the deflection at the load of the steel shaft as shown in figure 1: take  $E = 200$  Gpa [16]

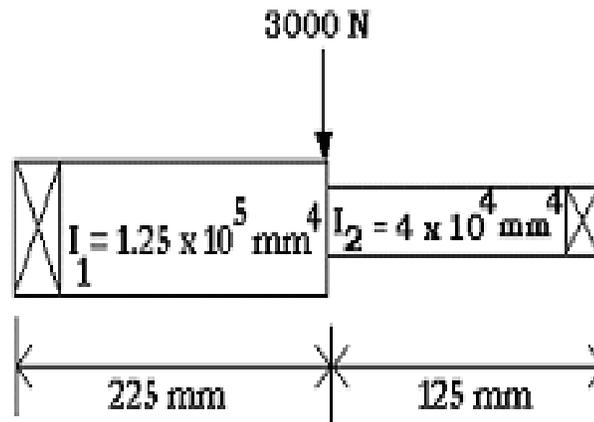


Figure 1:

4. Derive the shape functions for a triangular linear element in global Co-ordinate system. [16]
5. Derive the element conductivity matrix and load vector for solving 1- D heat conduction problems, if one of the surfaces is exposed to a heat transfer coefficient of  $h$  and ambient temperature of  $T_\infty$ ? [16]
6. Determine the natural frequencies of a simply supported beam of length 800 mm with the cross sectional area of 75 cm X 25 cm as shown in the figure2. Take  $E = 200$  Gpa and density of  $7850 \text{ kg/m}^3$ . [16]

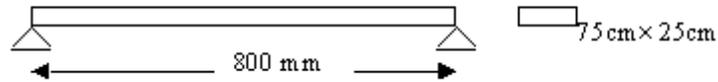


Figure 2:

7. Discuss about the following mesh generation methods
- (a) Mesh topology first.
  - (b) Nodes first.
  - (c) Adaptive mesh template.
  - (d) Nodes and elements simultaneously. [4+4+4+4]
8. With an example, explain the procedure involved in solving an engineering problem in computational finite element analysis using computer software. [16]

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